

**Please.** Do **not** approx.: If your result is " $\sin(\sqrt{\pi})$ " then write that rather than .9797... Use " $f(x)$  notation" when writing fncs; in particular, for trig and log fncs. E.g, write " $\sin(x)$ " rather than the horrible  $\sin x$  or  $[\sin x]$ . Write expressions unambiguously e.g, " $1/a + b$ " should be bracketed either  $[1/a] + b$  or  $1/[a + b]$ . (Be careful with **negative** signs!)

**Y4:** Show no work.

**z** Prof. King believes that writing in complete sentences aids in communicating technical ideas. Circle  
one: **True**      **What's a sentence?**      **DNE**

**a+** Let  $P_0 := (2\pi, 1, 2)$ . Compute the gradient of  $h(x, y, z) := xy + z \cdot \sin(x)$ .  
 $[\nabla h](P_0) =$  \_\_\_\_\_

Give an example of a *polynomial*  $f$  which has a saddle-point at  $(-8, 7)$ .

$f(x, y) :=$  \_\_\_\_\_

**b+** In  $\mathbb{R}^3$ , let  $S$  be the surface

$$6x - 3x^2 + 3 = 2y^2 + z^2.$$

Vector  $\mathbf{v} =$  \_\_\_\_\_  $\neq \mathbf{0}$  is  $\perp S$  at  $Q := (0, 1, 1)$ .  
\_\_\_\_\_

In form  $A[x - x_0] + B[y - y_0] + C[z - z_0] = 0$ , write an *equation* for the tangent plane to  $S$  at  $Q$ .

Eqn:

\_\_\_\_\_ Have arranged that  $A, B, C$  are **integers** with no common factor; also, that  $A \geq 0$ .

**c+** Let  $f(x, y) := x + 8y$ . Subject to the constraint that  $y^2 = x$ , compute the location  $(x_0, y_0)$  of a **global maximum** of  $f$ , and compute the location  $(x_1, y_1)$  of a **global minimum** of  $f$ .

Max = (\_\_\_\_\_, \_\_\_\_\_); Min = (\_\_\_\_\_, \_\_\_\_\_).

**d** An object in the first octant occupies the cube  $[0, L] \times [0, L] \times [0, L]$  The mass-density at each point in the cube is equal to the square of the point's distance from the origin, so the **total mass** of

the object is \_\_\_\_\_.

**Y5:** A box [rectangular parallelepiped] lies in the first octant, with three faces on the coordinate-planes and one vertex, agree to call it  $P$ , on the plane  $2x + y + 4z = 12$ . Use Lagrange Multipliers to compute the (unique) value of  $P$  which *maximizes* the *volume* of the box.

First, draw a large clear picture of the octant and the plane. Compute and label the  $x, y, z$ -intercepts of the plane, so that your picture is accurate. Now compute the four Lagrange equations: [The first eqn. is the constraint eqn.]

$C_f :$

$L_x :$

$L_y :$

$L_z :$

Now solve the system to compute [fill in the three blanks]  $P = ($  \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_).

End of Y-class

**Y-home:** \_\_\_\_\_ 460pts

**Y4:** \_\_\_\_\_ 180pts

**Y5:** \_\_\_\_\_ 50pts

**Total:** \_\_\_\_\_ 690pts

**HONOR CODE:** "I have neither requested nor received help on this exam other than from my professor (or his colleague)."  
*Name/Signature/Ord*

Ord: \_\_\_\_\_