

C1: ^{Mon.}_{27 Jan} a LBolt gives $G := \text{GCD}(23, 413) = \dots$. And

$23S + 413T = G$, where $S = \dots$ & $T = \dots$
are integers.

b Euler $\varphi(121000) = \dots$.

Express your answer as a product $p_1^{e_1} \cdot p_2^{e_2} \cdot \dots$ of primes
to posint powers, with $p_1 < p_2 < \dots$.

C3: *Magic integers* $G_1 = \dots$, $G_2 = \dots$,
 $G_3 = \dots$, each in $(-165..165]$, are st. mapping
 $g: \mathbb{Z}_6 \times \mathbb{Z}_5 \times \mathbb{Z}_{11} \rightarrow \mathbb{Z}_{330}$ is a ring-isomorphism, where

$$g((z_1, z_2, z_3)) := \left\langle z_1 G_1 + z_2 G_2 + z_3 G_3 \right\rangle_{330}.$$

Verify for your map: $g((1, 1, 1)) = 1$ and $[5 \cdot 11] \nmid G_1$ and
analogously for G_2 and G_3 .

C5: Bitstring “0101001010010001010100001”, via the
Elias code, decodes to $\dots$,
a sequence of *natnums* [hint: gun-blip-blip], followed by
noise-bits $\dots$.