

**Note.** Write chromatic polys in *chromatic form*.

**G4:** \_\_\_\_\_ 145pts

**G4:** Show no work. Write **DNE** in a blank if the described object does not exist or if the indicated operation cannot be performed.

**a** The vertex set of  $H_N$  is  $\mathbb{V} := [1..2N]$ . For  $\mathbf{u} \in \mathbb{V}$ , when possible:  $\mathbf{u} \rightarrow [\mathbf{u}+2]$ . If  $\mathbf{u}$  is odd, then  $\mathbf{u} \rightarrow [\mathbf{u}+1]$ . Thus

$\mathcal{P}_{H_N}(x) =$   
.....  
And  $H_N$  has \_\_\_\_\_ acyclic orientations.

**b** Glue a vertex of  $C_5$  to an endpoint of  $P_3$ , to form a 7-vertex graph  $D$ . The number of two-component spanning subgraphs of  $D$  is \_\_\_\_\_.

**c** Graph  $G$  has chromatic polynomial

$$x^9 - 10x^8 + 44x^7 - 112x^6 + 182x^5 - 196x^4 + 139x^3 - 60x^2 + 12x.$$

Our  $G$  has \_\_\_\_\_ spanning subgraphs. Of those that are connected, ten of them have oddly-many edges, and thus \_\_\_\_\_ of them have evenly-many edges. [Hint: Chromatic-Polynomial Spanning Subgraph Thm]

**d** Graph  $S := W_5 \odot C_6$ , the full-product of the 5-vertex wheel with the 6-cycle, has \_\_\_\_\_ edges.

And  $\chi(S) =$   
.....

**e** Full-product,  $\odot$ , is associative.  $T \odot F$   
Graph  $[K_2 \odot K_3] \odot K_4$  has chromatic polynomial  
.....

**f** There are \_\_\_\_\_ trees on vertex-set  $[1..7]$ .  
.....