



Staple!

Geometry  
MTG3214 03H9

## Class-B

Prof. JLF King  
3Sep2015

End of Class-B

**B1:** Short answer. Show no work.

Please write DNE in a blank if the described object does not exist or if the indicated operation cannot be performed.

**a** With  $A := (0, 1)$ ,  $B := (2, 3)$ ,  $C := (7, 1)$ , let  $T$  denote  $\triangle ABC$ . Then  $\text{OrthoCenter}(T) = ( \underline{\hspace{2cm}}, \underline{\hspace{2cm}} )$ .

**a'** The above  $T$  is the medial triangle of  $\triangle PQR$ , where  $P = ( \underline{\hspace{2cm}}, \underline{\hspace{2cm}} )$  has the most-positive  $x$ -coordinate.

**b** Triangle  $\triangle EFG$  has  $\text{Len}(\overline{EF}) = 7$ ,  $\angle FGE = 35^\circ$  and  $\text{Len}(\overline{GF}) = 17$ . This data is consistent with  circle

0      1      2       $\infty$ 

many triangles.

OYOP: In grammatical English sentences, write your essays on every third line (usually), so that I can easily write between the lines. Do not restate the question.

In your essays, you may use the following proposition for free.

**1: AAA-Prop.** For  $j = 1, 2$ , consider triangles  $\mathbf{S}_j := \triangle E_j F_j G_j$ . If corresponding angles are equal [ $\angle E_1 F_1 G_1 = \angle E_2 F_2 G_2$ , etc.] then  $\mathbf{S}_1$  is similar to  $\mathbf{S}_2$ .  $\diamond$

**B2:** Consider a circle  $\Omega$  and a point  $U$  outside of  $\Omega$ . A ray from  $U$  intersects  $\Omega$  first at a point  $B$  and then at  $C$ . Another ray from  $U$  intersects  $\Omega$  at  $Q$ , then  $R$ . [See diagram on blackboard. Points  $B, C, Q, R$  are distinct.] Prove that  $\triangle UBR$  is similar to  $\triangle UQC$ .

**B3:** Carefully state the Euler-line theorem for a triangle  $\mathbf{S} := \triangle PQR$ .

Write a careful proof the Euler-line thm, stating and proving any lemmas you need.

**B1:** \_\_\_\_\_ 65pts**B2:** \_\_\_\_\_ 55pts**B3:** \_\_\_\_\_ 75pts**Total:** \_\_\_\_\_ 195pts