

Hello. Please write **DNE** in a blank if the described object does not exist or if the indicated operation cannot be performed.

B1: Show no work.

Z $\lim_{\text{GPA} \rightarrow 0} \begin{bmatrix} \text{Engineering} \\ \text{student} \end{bmatrix}$ equals (Circle one):

Business major “For Here Or To Go?” Dental-floss designer

(The Business school has a *different* version of this joke...)

a In \mathbb{R}^3 , the point $P := (3, 1, -2)$ has orthogonal projection $\text{Proj}(P) = (\underline{\dots}, \underline{\dots}, \underline{\dots})$ on the line passing through $(20, 40, 20)$ and the origin.

b Open \mathbb{R} -intervals $J_n := (\underline{\dots}, \underline{\dots})$ intersect to a “half-open” nv-interval $\bigcap_{n=1}^{\infty} J_n = (\underline{\dots}, \underline{\dots}]$.

c' Let $S := \{q \in \mathbb{Q}_+ \mid 4 < q^2 \leq 7\}$. Then:
 $\text{Cl}_{\mathbb{R}}(S) = \underline{\dots}$. $\text{It}_{\mathbb{R}}(S) = \underline{\dots}$.
 $\text{Cl}_{\mathbb{Q}}(S) = \underline{\dots}$. $\text{It}_{\mathbb{Q}}(S) = \underline{\dots}$.

d Let $S := \{q \in \mathbb{Q}_+ \mid 4 < q^2 \leq 7\}$. Then:
 $\text{Bdry}_{\mathbb{R}}(S) = \underline{\dots}$. $\text{Bdry}_{\mathbb{Q}}(S) = \underline{\dots}$.

e On \mathbb{Z} , say $k \mathrel{\$} n$ IFF $k - n$ is a multiple of 6. Then $\$$ is: **Trans.**: $\mathcal{T} \mathcal{F}$. **Symm.**: $\mathcal{T} \mathcal{F}$. **Refl.**: $\mathcal{T} \mathcal{F}$.

B2: Show no work. **i** Give an example of a set,

$$\left\{ \underline{\dots} \in \mathbb{R} \mid \underline{\dots} \right\},$$

which has $5 \in \mathbb{R}$ as its only \mathbb{R} -cluster point.

ii Suppose that U, V_1, V_2, \dots are \mathbb{R} -open-sets, and E, K_1, K_2, \dots are \mathbb{R} -closed-sets. those of the following sets which are guaranteed to be \mathbb{R} -closed.

$$E \setminus U. \quad K_1 \setminus E. \quad \bigcap_{n=1}^{\infty} K_n.$$

$$\mathbb{R} \setminus \left[\bigcup_{n=1}^{\infty} V_n \right]. \quad [U \cap V_1]^c.$$

Essay questions: For each question, carefully write a triple-spaced essay solving the problem.

Each essay starts a new page.

B3: In MS (Ω, d) , sequence $\vec{b} \subset \Omega$ converges to both q and r in Ω . Prove that $q = r$, by showing that $d(q, r) = 0$. [Hint: Use the Triangle Inequality.]

B4: Use $\langle \cdot, \cdot \rangle$ for an inner-product on real vectorspace \mathbf{V} . Carefully state the Cauchy-Schwarz Inequality Theorem, making precise the IFF-condition for equality. If you use a term such as “orthogonal” or “linearly independent” or “parallel”, then *define* it precisely in terms of the inner-product and/or the vectorspace operations.

End of Class-B

B1: 95pts

B2: 25pts

B3: 50pts

B4: 25pts

No name, or
no honor code: -5pts

Unstapled, or
no ordinal : -5pts

Total: 195pts

Please PRINT your **name** and **ordinal**. Ta:

Ord:

HONOR CODE: *I have neither requested nor received help on this exam other than from my professor.*

Signature: